Ensemble forecasting and data assimilation: two problems with the same solution?

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1. Introduction

Until 1991, operational NWP centers used to integrate a single control forecast starting from the analysis, which is the best estimate of the state of the atmosphere at the initial time. In December 1992, both NCEP and ECMWF started running *ensembles* of forecasts from slightly perturbed initial conditions (Molteni and Palmer, 1993, Buizza, 1997, Toth and Kalnay, 1993, Tracton and Kalnay, 1993, Toth and Kalnay, 1997).

Ensemble forecasting provides human forecasters with a range of possible solutions, whose average is generally accurate than the more sinale deterministic forecast (see, e.g., Fig. 4), and whose spread gives information about the forecast errors. It also provides а quantitative basis for probabilistic forecasting.

Schematic Fig. 1 shows the essential components of an ensemble: a control forecast started from the analysis, forecasts started from two perturbations to the analysis (in this case equal and opposite), the ensemble average, and the "truth", or forecast verification, which becomes available later. The first schematic shows an example of a "good ensemble" in which "truth" looks like a member of the ensemble. In this case, the ensemble average is closer to the truth, due to nonlinear filtering of errors, and the ensemble spread is related to the forecast error. The second schematic is an example of a "bad ensemble": due to poor initial

perturbations and/or model deficiencies, the forecasts are not able to track the verifying truth, and remain relatively close to each other. In this case the not helpful to ensemble is the forecasters at all, since the lack of ensemble spread would give them uniustified confidence in the erroneous forecast. Nevertheless, for NWP development, the "bad" ensemble is still very useful: after the verification time arrives, it clearly indicates the presence of a deficiency in the forecasting system. A single "deterministic" forecast, by contrast, would not be able to distinguish between a deficiency in the system and errors in the initial conditions as the cause of failure.

Ideally, the initial perturbations should sample well the analysis "errors of the day" and the spread among the ensemble members should be similar to that of the forecast errors. The two essential problems in the design of an ensemble forecasting system are how to create effective initial perturbations, and how to handle model deficiencies, which make the ensemble forecast spread smaller than the forecast error.

In this paper we present a brief historic review of ensemble forecasting, current methods to create perturbations. We point out that the promising approach of ensemble Kalman Filtering for data assimilation can solve, at the same time, the problems of obtaining optimal initial ensemble perturbations, and possibly estimating the impact of model errors. We also discuss the problem of coupled systems with instabilities that have very different time scales.

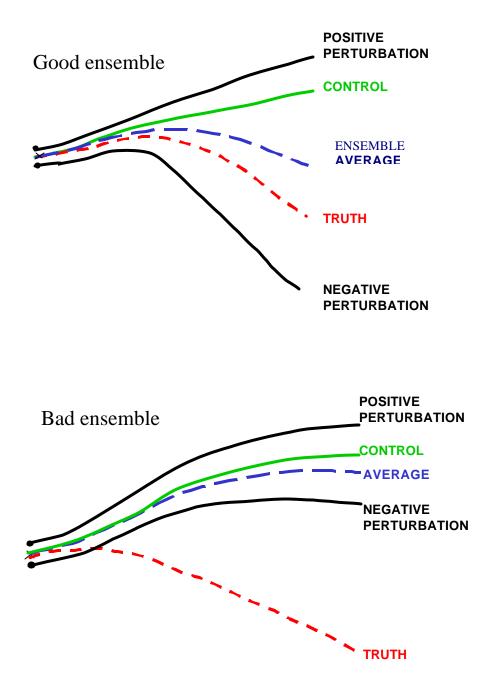


Figure 1: Schematic of the essential components of an ensemble of forecasts: The analysis (a cross) which constitutes the initial conditions for the control forecast (in green); the initial perturbations (a thick dot) around the analysis, which in this case are chosen to be equal and opposite; the perturbed forecasts (in black); the ensemble average (in blue); and the verifying analysis or truth (in red). The first schematic is that of a "good ensemble" in which the truth is a plausible member of the ensemble. The second is an example of a bad ensemble, quite different from the truth, pointing to the presence of a problem in the forecasting system such as deficiencies in the analysis, in the ensemble perturbations and/or in the model.

It should be noted that human forecasters have always performed subjective ensemble forecasting by checking forecasts from previous days, and comparing forecasts from different centers, approaches similar to lagged forecasting and multiple systems forecasting. The consistency among these forecasts at a given verification time provided a level of confidence in the forecasts, confidence that changed from day to day and from region to region.

2.1 Early methods

Epstein (1969), introduced the idea of Stochastic-Dynamic forecasting (SDF), and pointed out that it could be also used in the analysis cycle to provide the forecast error covariance. Epstein designed SDF as a shortcut to estimate the true probability distribution of the forecast uncertainty, given by the Liouville equation (Ehrendorfer, 2002), which Epstein approximated running a huge (500) number of perturbed (Monte Carlo) integrations for the 3-variable Lorenz (1963) model. However, since SDF involves the integration of forecast equations for each element of the covariance matrix, this method is still not computationally feasible for models with large number of degrees of freedom.

Leith (1974) suggested using directly a Monte Carlo Forecasting approach (MCF), where random perturbations sampling the *estimated* analysis error covariance are added to the initial conditions. He noted that in an infinitely large ensemble, the average forecast error variance at long time leads converges to the climatological error variance, whereas the error variance of individual forecasts converges to twice the climatological error variance. Leith showed that with just a relatively small number of integrations (of the order of 8) it is possible to approximate this important advantage of an infinite ensemble. The estimate of the analysis error covariance was constant in time. so the MCF method did not include the effects of "errors of the day". The MCF method is shown schematically in Fig. 2a. Errico and Baumhefner (1987) applied this method to realistic global models. using perturbations that represented a realistic (but constant) estimation of the errors in the initial conditions. Hollingsworth (1980) showed that random errors in the initial conditions took too long to spin-up into growing "errors of the day", making MCF an inefficient approach for ensemble forecasting.

Hoffman and Kalnay (1983) suggested as an alternative to MCF, the Lagged Averaged Forecasting (LAF) method, in which forecasts from earlier analyses were included in the ensemble (schematic Fig. 2b). Since the ensemble members are forecasts of different "ages" they should be averaged with weights estimated from their average forecast errors. Hoffman and Kalnay found that compared to MCF, LAF resulted in a better prediction of skill (a stronger relationship between ensemble spread and error), presumably because LAF includes the effect of variable of the dav". "errors The main disadvantage of LAF, that the "older" forecasts are less accurate, was corrected by the Scaled LAF (SLAF) approach of Ebisuzaki and Kalnav (1991), in which the LAF perturbations (difference between the forecast and the current analysis) are scaled by their "age", so that all the SLAF perturbations have errors of similar magnitude. They also that the scaled suggested perturbations should be both added and subtracted from the analysis, thus increasing the ensemble size and the probability of "encompassing" the true solution within the ensemble. SLAF can be easily implemented in both global and regional models, including the impact of perturbed boundary conditions (Hou et al, 2001).

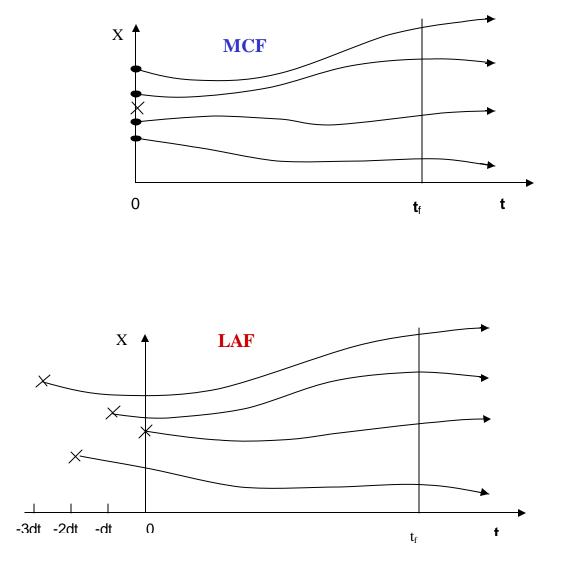


Fig. 2: Schematic of the Monte Carlo forecasting and Lagged Average Forecasting methods.

In December 1992 two methods to create perturbations became operational at NCEP and at ECMWF. They are based on bred vectors and singular vectors respectively, and like LAF, they include "errors of the day". These and other methods that have since become operational or are under consideration in operational centers are briefly discussed. More details are given in Kalnay (2003).

a. Singular Vectors (SVs)

Singular vectors the linear are perturbations of a control forecast that grow fastest within a certain time interval (Lorenz, 1965), known as "optimization period", using a specific norm to measure their size. SVs are strongly sensitive to the length of the interval and to the choice of norm (Ahlauist. 2000). Ehrendorfer and Tribbia (1997) showed that if the initial norm used to derive the singular vectors is the analysis error covariance norm, then the initial singular vectors evolve into the eigenvectors of the forecast error covariance at the end of the optimization period. This indicates that if the analysis error covariance is known. then singular vectors based on this specific norm are the ideal perturbations.

ECMWF implemented an ensemble system with initial perturbations based on singular vectors using a total energy norm (Molteni and Palmer, 1993, Molteni et al, 1996, Buizza et al, 1997, Palmer et al 1998).

b. Bred Vectors (BVs)

Breeding is a nonlinear generalization of the method to obtain leading Lyapunov vectors, which are the sustained fastest growing perturbations (Toth and Kalnay,

1993, 1997). Bred Vectors (like the leading Lvapunov Vectors) are independent of the norm and represent the shapes of the instabilities arowing upon the evolving flow. In areas where the evolving flow is very unstable (and where forecast errors grow fast), the BVs tend to align themselves along very low dimensional subspaces (the locally most unstable perturbations, Patil et al, 2001). An example of such situation is shown in Figs. 3, where the forecast uncertainty in a 2.5 day forecast of a storm is very large, but the subspace of the ensemble uncertainty lies within a one-dimensional space. In this extreme (but not uncommon) case, a single observation at 500hPa would be able to identify the best solution!

The bred vectors are the differences between the forecasts (the forecast perturbations). In unstable areas of fast growth, they tend to have shapes that are independent of the forecast length or the norm, and depend only on the verification time. This suggests that forecast errors, to the extent that they reflect instabilities of the background flow, should have shapes similar to bred vectors, and this has been confirmed with model simulations (Corazza et al, 2002).

NCEP implemented an ensemble system based on breeding in 1992. Later, the US Navy, the National Centre for Medium Range Weather Forecasting in India, and the South African Meteorological Weather Service implemented similar ensemble forecasting systems. The Japanese Meteorological Agency ensemble forecasting system is also based on breeding, but imposing a partial global orthogonalization among the bred vectors, thus reducing the tendency of the bred vectors to converge towards a low dimensional space of the most directions unstable (Kyouda and Kusunoki, 2002).

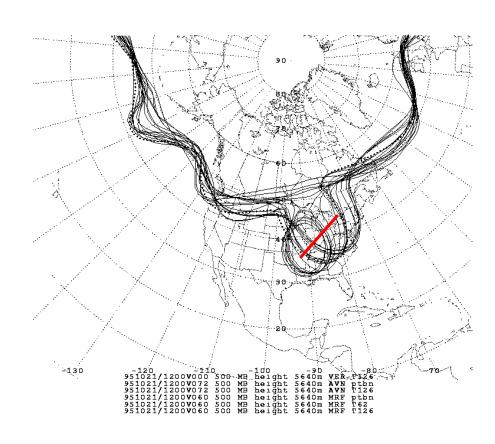


Fig. 3: "Spaghetti plots" showing a 2.5 day ensemble forecast verifying on 95/10/21. Each 5640gpm contour at 500 hPa corresponds to one ensemble forecast, and the dotted line is the verifying analysis. Note that the uncertainty in the location of the center of the predicted storm in SE US is very large, but that the differences among forecasts of the storm lie on a 1-dimensional space (red line).

Houtekamer et al (1996) developed a system based on running an ensemble of data assimilation systems using perturbed observations, implemented in the Canadian Weather Service. Hamill et al (2000) showed that in a guasigeostrophic system, a multiple data assimilation system performs better than the singular vectors and the breeding approaches. With respect to the computational cost, the multiple data assimilation system and the singular approach are comparable. vector whereas breeding is essentially costfree.

c. Multiple data assimilation systems

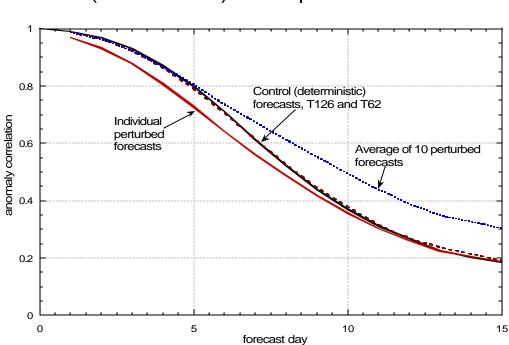
d. Perturbed physical parameterizations

The methods discussed above only include perturbations in the initial conditions, assuming that the error arowth due to model deficiencies is small compared to that due to unstable growth of initial errors. In addition, several aroups have introduced changes in the physical parameterizations to allow for the inclusion of model uncertainty (Houtekamer et al, 1996, Stensrud et al, 2000). Buizza et al (1999)developed а perturbation approach that introduces a stochastic perturbation of the impact of subgrid scale physical parameterizations by simply multiplying the time derivative of the "physics" by a random number normally distributed with mean 1 and standard deviation 0.2.

e. Multiple system ensembles

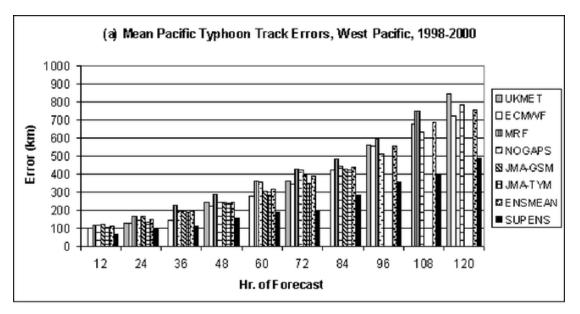
Both the perturbations of the initial conditions and of the subgrid scale physical parameterizations have been shown to be successful towards achieving the goals of ensemble forecasting. However, since they both introduce perturbations in the best estimate of the initial conditions and the model, which are in the control forecast, it can be expected that the individual perturbed forecasts should be worse than the control. A typical ensemble average for a season (Figure 4) shows that, indeed, the individual perturbed forecasts have less skill than the unperturbed control. Nevertheless, the ensemble average is an improvement over the control, especially after the perturbations grow into a nonlinear regime that tends to filter out some of the errors.

An alternative to the introduction of perturbations is the use of multiple systems developed independently at different centers. In principle, an ensemble of forecasts from different operational or research centers, each aiming to be the best and choosing different competitive approaches, should sample well the uncertainty in our knowledge of both the models and the initial conditions. It has long been known that the ensemble average of multiple center forecasts is significantly better than even the best individual forecasting system (e.g., Kalnay and Ham, 1989, Fritsch et al, 2000, Arribas et al, 2004). This has also been shown to be true for regional models (Hou et al. 2001). (1999) introduced the Krishnamurti concept of "superensemble", using linear regression and past forecasts of different systems as predictors to minimize the ensemble average prediction errors. This results in remarkable forecast improvements (e.g., Fig. 5). This method is also called "poor person's" method to reflect that it does not require running a forecasting system.



Anomaly Correlation for the winter of 1997/98 (from 00Z) Controls (T126 and T62) and 10 perturbed ensemble forecasts

Fig. 4: Anomaly correlation of the ensembles during the winter of 1997/1998 (data courtesy Jae Schemm, of NCEP).



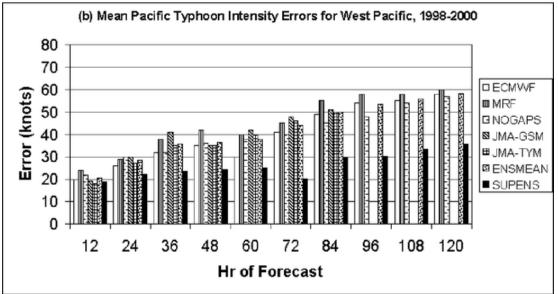


Fig. 5: Mean typhoon track and intensity errors for the west Pacific, 1998-2000 for several global models and a superensemble trained on the first half of the same season (Kumar et al, 2003). The forecasts are verified on the second half of the season.

f. Other methods

This field is changing guickly, and improvements and changes to the operational systems are under development. For example, ECMWF has implemented changes in the length of the optimization period for the SVs, a combination of initial and final or evolved SVs (which are more similar to BVs), and the introduction of a stochastic element in the physical parameterizations. all of which contributed to improvements in the ensemble performance. NCEP is considering the implementation of the Ensemble Transform Kalman Filter (Bishop et al, 2001) to replace breeding 3). (see also section Α recent comparison of the ensemble performance of the Canadian. US and ECMWF systems (Toth et al., 2004) suggests that the ECMWF ensembles based on singular vectors behave well beyond the optimization period, at which time the model advantages of the ECMWF system are also paramount. The NCEP bred vectors are better at ranges. and the shorter multiple analyses Canadian method also seems to perform well.

3. Ensemble Kalman Filtering for data assimilation and ensemble forecasting.

As indicated before (e.g., Ehrendorfer and Tribbia, 1997), "perfect" initial perturbations for ensemble forecasting should sample well the analysis errors. The ideal initial perturbations d x: should have а covariance that represents the analysis error covariance A:

$$\frac{1}{K-1}\sum_{i=1}^{K} d\mathbf{x}_{i} d\mathbf{x}_{i}^{T} \approx \mathbf{A}$$
(1.1).

Until recently, the problem has been that we do not know A, which changes substantially from day to day and from region to region due to instabilities of the background flow. These instabilities, associated with the "errors of the day", are not taken into account in data assimilation systems, except for 4D-Var and Kalman Filtering, methods that are computationally very expensive. 4D-Var has been implemented at ECMWF and at MeteoFrance (Rabier et al. 2000. Andersson et al, 2004), with some simplifications such as reducing the resolution of the analysis in order to reduce the computational cost (from ~40km in the forecast model to ~120km in the assimilation model). Versions of 4D-Var are also under development in other centers.

The original formulations of Kalman Filtering (Kalman, 1960) and Extended Kalman Filtering (Ghil and Malanotte-Rizzoli. 1991. Cohn. 1997) are prohibitive in practice because they would require the equivalent of N model integrations, where N is the number of degrees of freedom (d.o.f.) of the model, which is of the order of a 10⁶ or more. Considerable work has been done on finding simplifying assumptions to reduce the cost of KF (e.g., Fisher, 1998, Fisher et al, 2003), but so far they have been successful only under special circumstances.

Ensemble Kalman Filtering (EnKF) was introduced by Evensen (1994) as a more efficient approach to Kalman Filtering. Recent developments suggest that in the near future it will be feasible to determine simultaneously the covariance matrix **A** and the ideal perturbations $d\mathbf{x}_i$. These methods take advantage of the fact that the size of ensembles needed to represent the analysis and forecast error covariances

is of order O(100), much smaller than the number of degrees of freedom of the model. When EnKF is performed locally in physical space (Ott et al, 2002), the number is smaller than 100.

There are two basic approaches to EnKF. In the first one (known as "perturbed observations") an ensemble of data assimilations is carried out using the same observations to which random have been added. The ensemble is used to estimate the forecast error covariance needed in the Kalman Filter (Evensen. 1994. Houtekamer and Mitchell, 1998, Hamill and Snyder, 2000). This approach has already been shown to be very competitive with the 3D-Var. operational an important milestone, given that 3D-Var has the of benefit vears of improved developments (Houtekamer et al, 2004).

The second approach is the class of square root filters (Tippett et al, 2002), and does not require perturbing the observations. Several groups have recently independently developed square root filters (Bishop et al, 2001, Anderson, 2001, Whitaker and Hamill, 2002, Ott et al, 2002). The ensemble forecasts are used to obtain а background error covariance at the time of the analysis. The full Kalman Filter equations and the new observations are then used to obtain the analysis increment (difference between the analysis and the forecast) and the analysis error covariance, all lying within the subspace of the forecast ensemble. After this is completed, the new initial analysis perturbations dx are obtained by solving the square root problem of equation (1.1), and the analysis cycle can continue.

Several of the Ensemble Kalman Filters further reduce the computational cost by assimilating the observations one at a time, for the whole physical domain, a method known as sequential assimilation of observations. This is done using a localization of the error covariance in the horizontal and in the vertical, to avoid spurious long-distance correlations due to sampling.

In the Local Ensemble Kalman Filter (LEKF) method (Ott et al, 2002, 2004, Szunyogh et al, 2004a, b), the Ensemble Kalman Filter problem is solved locally in physical space. For each grid point a local 3D volume of the order of 1000km by 1000km and a few vertical lavers is used to perform the analysis. The Kalman Filter equations are solved exactly on this subspace locally spanned by the global ensemble members, using all the observations available within the volume. This localization in space results in a further reduction of the number of necessary ensemble members, so that matrix operations are done in a very low dimensional space. The analysis is carried out independently at each grid point, with essentially perfectly parallel computations.

In order to visualize the main advantage of Ensemble Kalman Filtering (EnKF), we compare it with the 3D-Var approach currently operational in most centers, in which the analysis error covariance is estimated as an average over many cases. The top schematic Fig. 6 shows how the 3D-Var analysis maximizes the ioint probability defined bv the observations error covariance and the background error covariance, but does not know about "errors of the day". The bottom schematic shows how in the EnKF, the ensemble perturbations defines a low-dimensional subspace (10-100).and the KF analvsis maximizes the joint probability within this subspace. Because all the computations are performed within this subspace, the rank of the matrices involved is low, and the Kalman Filter equations providing the analysis and

analysis error covariance are solved directly, not iteratively.

Fig. 7 shows an example of EnKF and 3D-Var using a quasi-geostrophic data assimilation system (Morss et al, 2000, Hamill and Snyder, 2000, Corazza et al, 2002). The colors show the background (12 hour forecast) errors and the contours are the analysis corrections based on a given set of observations. The top panel corresponds to 3D-Var, using a background error covariance constant in time. Since the system does not know about the "errors of the day", the corrections brought by the new observations tend to be isotropic. The bottom panel shows that the Local Ensemble Kalman Filter (Ott et al, 2004, Szunyogh et al, 2004b) is much more efficient in correcting the background errors with the same observations. The large improvements that the LEKF makes on the analysis are also apparent in the 3-day forecasts (not shown).

Performing the EnKF locally in space substantially reduces the number of ensemble members required for the analysis, as shown with experiments done with the Lorenz (1996) model (Fig. 8, from Ott et al, 2004). When performed globally, the number of ensemble members required for the EnKF to converge is proportional to the size of the model. When done locally, the number of ensemble members is reduced from 27 to 8, and does not increase with the size of the model. In addition, the analysis for different grid points can be carried out in parallel, since they are independent from each other. The advantage of a local analysis in reducing the size of the required ensemble is illustrated in Fig. 9, showing a schematic of an ensemble with three independent unstable regions. In each of the regions wave number 1 and 2 are unstable. This situation is reminiscent of the global atmosphere. containing regions where baroclinic instabilities can develop independently. From a local point of view, the first two perturbations are enough to represent all possible combinations of instabilities, whereas from a global point of view, the third perturbation and many others are linearly independent.

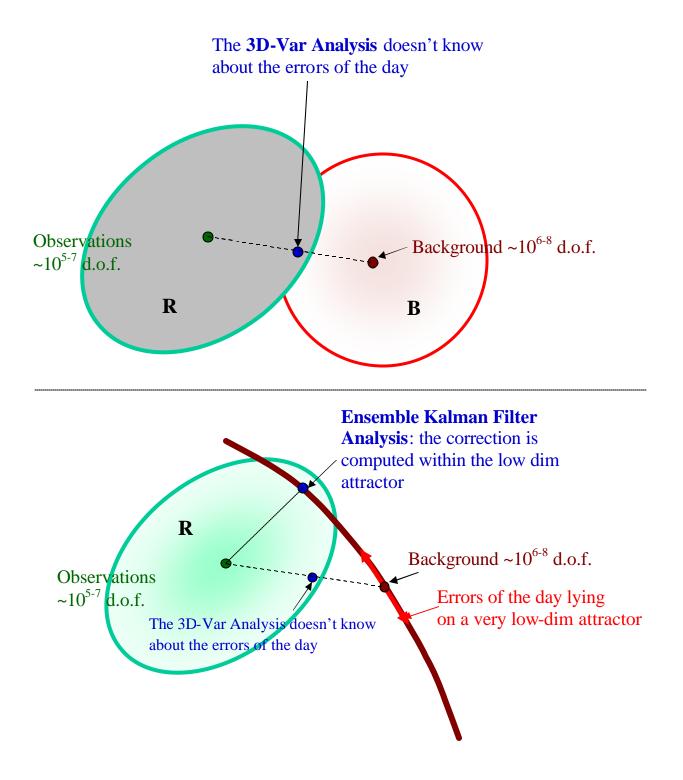
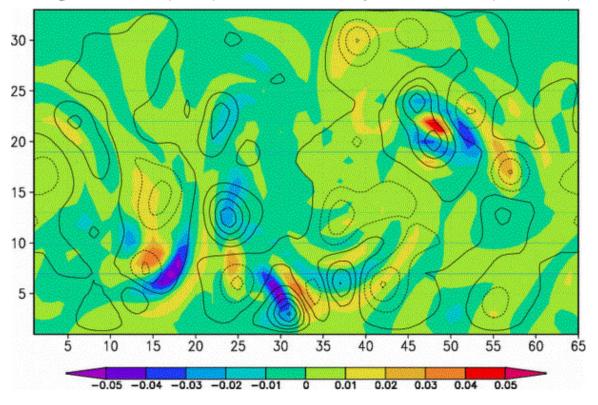


Figure 6: Schematic of the analysis given the background forecast in a very large dimensional space, the background error covariance **B** (which in the case of 3D-Var is isotropic and constant in time), the vector of observations, in a very large dimensional space, with observations error covariance **R**. The analysis estimate of the true state of the atmosphere maximizes the joint probability distribution. Top: 3DVar. Bottom: EnKF, in which the ensemble forecast members define a low-dimensional subspace within which the analysis lies.

Background error (color) and 3D- Var analysis increment (contours)



Background error (color) and LEKF analysis increments (contours)

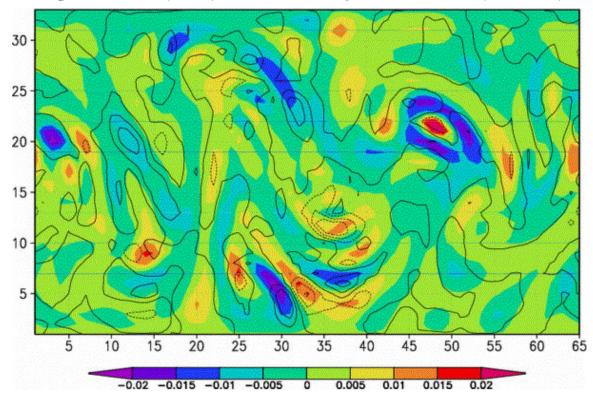


Fig. 7: Simulation of data assimilation in a quasi-geostrophic model, assimilating potential vorticity observations at a particular day (June 15). The color represents the 12 hr forecast (background) error and the contours the analysis corrections. Top: 3D-Var. Bottom: Local Ensemble Kalman Filter. Figures courtesy of Matteo Corazza.

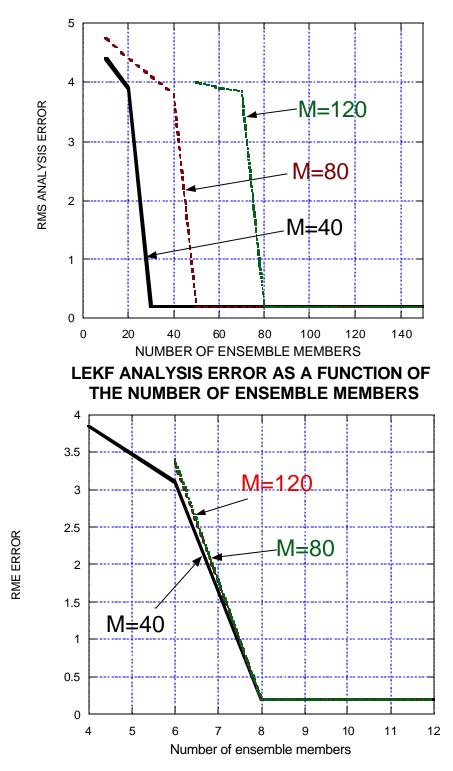


Fig. 8: Number of ensemble members required for convergence to the optimal solution in a Lorenz (1996) model. Top: using a full global Ensemble Kalman Filter. Bottom: using a Local Ensemble Kalman Filter. The size of the domain, M is 40, 80 or 120. Note that the Kaplan-Yorke dimension is about 27 for the 40 variable model and it increases linearly with size.

FULL ENSEMBLE KALMAN FILTER ANALYSIS ERROR AS A FUNCTION OF THE NUMBER OF ENSEMBLE MEMBERS

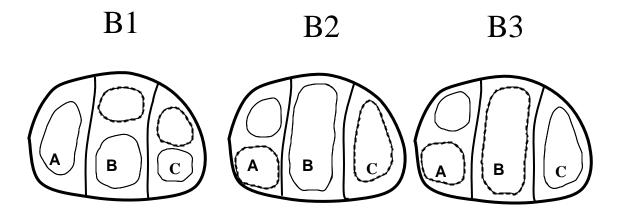


Fig. 9: Schematic showing the advantages of performing a local rather than a global analysis. The domain in composed of three regions, each of which has instabilities with wave numbers 1 and 2, positive (solid) or negative(dashed). From a local point of view, the ensemble perturbations B1 and B2 are sufficient to represent all possible perturbations, whereas from a global point of view there are many independent perturbations.

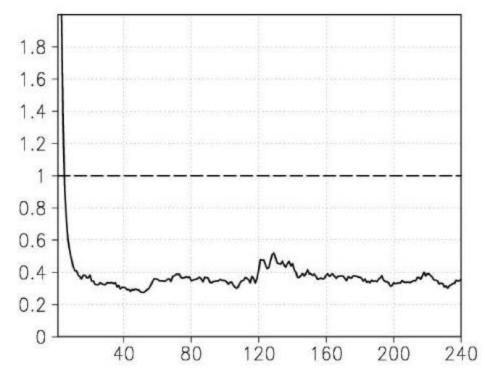


Fig. 10: Evolution of the LEKF analysis error in surface pressure in hPa as a function of assimilation step (in units of 6 hr). The rms error of the observations is shown by the dashed line. Observations are made at 11% of the grid points, and the model has T62 (about 200km) resolution. (From Szunyogh et al, this volume)

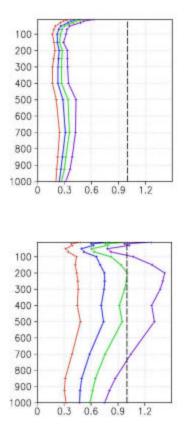
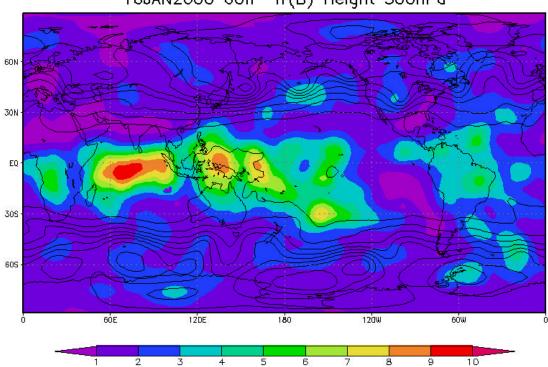


Fig. 11: Global rms analysis error for temperatures (left, °C) and zonal winds (right, m/sec). The dashed line is the rms of observational errors. From left to right, the following percentage of the grid points have "rawinsonde" data: 100% (red), 11% (blue), 5% (green), 2% (purple). Since the grid resolution is about 200km, the blue is similar to the current rawinsonde density in the NH, and the purple to the SH and tropics. (From Szunyogh et al, this volume)

Fig. 12: Example of the trace of the 6hr forecast error covariance matrix from the LEKF. It indicates where errors are large or small: regions in purple do not need new observations because the uncertainties are small. This information can be used in adaptive observations.



16JAN2000 00h Tr(B) Height 500hPa

The LEKF has been tested in a "perfect model" mode, using the operational NCEP Global Forecasting System at T62/28levels resolution, with excellent results (Szunyogh et al, 2004b, this volume). Fig. 10 shows the evolution of the analysis of surface pressure, when about 11% of the grid points (separated by about 200km) have "rawinsonde" observations of surface pressure, and vertical profiles of temperature and winds, with random errors of 1hPa, 1K and 1m/s on each wind component. Similarly to the rapid reduction of global analysis rms error for surface pressure in this figure, the analysis errors for temperature and winds quickly converge to values much smaller than the observational errors (not shown). Fig. 11 shows the vertical rms analysis errors for temperature and winds for several levels of observational density, from 11% of the grid points, a density similar to that of the rawinsondes in the NH extratropics, to 2%, a density similar to rawinsondes in the SH. The ability of the LEKF to extract information through the knowledge of the "errors of the day" is very encouraging.

Although experiments with real observations have not yet been completed, the LEKF shows great promise: 1) it is very efficient, due to its complete parallelism and need for relatively few ensemble members, allowing for a direct rather than iterative solution. It takes only 15 minutes to assimilate 1.5 million observations using 40 ensemble members on a cluster of 25 dual processor 2.8 GH PCs: 2) like all EnKF methods, LEKF does not require the creation and maintenance of the forecast model's linear tangent or adjoint models, saving the very large effort that these models usually require. avoids lt also many required simplifications, since the full nonlinear model is used for every operation. Similarly it does not require the Jacobian or the adjoint of the

observation operator Н. another important advantage (Takemasa Miyoshi, 2004, pers. communication). 3) It can be easily extended to 4 dimensions, so that observations are assimilated correctly even if their time of observation falls in between analysis times (Sauer et al, 2004). This 4D LEKF is performed at a low additional computational cost using the ensemble to "transport" observational increments from the time of observation to the analysis time. This is important since experience indicates that the ability to assimilate observations at the right time is the main advantage of 4D-Var (rather than the evolution of the covariance). Another advantage of EnKF is the precise way it allows to perform adaptive observations: Fig. 12 shows an example of the trace of the background error covariance for a given day of the LEKF data assimilation simulation. This provides a clear estimate of the forecast uncertaintv. This field. and the corresponding analysis uncertainty can contrasted with the analysis be increments as a "reality check". The LEKF could eventually be computed alongside a satellite instrument, such as a wind lidar, and provide an indication of where there is a large analysis/forecast error and the instrument should dwell longer, and where observations are not currently needed.

4. Summary and some remaining problems

In summary, ideal initial ensemble perturbations should span effectively the analysis error covariance, as in equation (1.1). Until recently, this was an apparently impossible task, since the analysis error covariance was unknown. Methods such as breeding and singular vectors were devised as shortcuts to (1.1). However, Ensemble Kalman Filtering holds the promise of solving both the data assimilation and the ensemble forecasting problem

simultaneously, since both the lhs and the rhs of this equation are obtained durina EnKF assimilation. the Furthermore, experience with the NCEP global model indicates that it is possible to carry out this advanced approach with supercomputers present day and without sacrificing the resolution of the analysis model. Additional advantages are that the linear tangent and adjoints codes of the forecast model or the observation operators are not needed. and that atmospheric data can be assimilated at the time they were observed.

One of the most important remaining problems is that of model deficiencies, leading to bias in data assimilation (Dee and DaSilva, 1999), to systematic forecast errors, and to ensemble deficiencies such as indicated in Fig. 1b. Obviously, the ultimate solution to this problem lies in the improvement of the models (e.g., Simmons and Hollingsworth, 2002), but until that stage is reached, empirical approaches may be needed.

А successful approach to start addressing the problem of errors and uncertainties in the model is the use of multiple models (Krishnamurti 1999, Hou et al. 2001, Fritsch, 2001, Kalnav and Ham, 1989). Other approaches (DelSole and Hou, 1999, Kaas et al, 1999) rely on empirical statistical methods to modify the model and reduce forecast errors. In another method, known as "dressing", random perturbations are added to the ensemble forecasts in order to reproduce the observed error covariance with an enhanced ensemble forecast spread (Roulston and Smith, 2003, Wang and Bishop, 2004).

It is possible that the Ensemble Kalman Filtering approach will also be able to efficiently minimize model errors by augmenting the space of model variables with a relatively small number of parameters associated with model errors, and using the observations to estimate the optimal value of their timevarying coefficients (e.g., Anderson, 2001).

Another important problem in ensemble forecasting and data assimilation arises with the presence of coupled instabilities with a wide range of time scales. For example, atmospheric convection, baroclinic instabilities, and the ENSO instabilities of the coupled oceanatmosphere system are characterized by time scales of minutes, days and months respectively.

This difficult problem of belquo systems (Timmerman, 2002) has been allowing attacked bv fast. small amplitude modes to saturate (Toth and Kalnay, 1993, Aurell et al, 1996, Boffetta et al, 1998). Toth and Kalnay (1993, 1996) proposed that breeding with rescaling amplitudes above the saturation level could be used to filter fast, small amplitude instabilities such as convection, without the need to eliminate or simplify their physical impact. Conversely, the choice of very small amplitudes for the rescaling can identify the bred vectors dominated by This coniecture convection. was validated by Lorenz (1996), and Peña and Kalnay (2004).

Unfortunately, In the case of the coupled ocean-atmosphere svstem. the "atmospheric weather noise" has larger, not smaller amplitudes than the slow ENSO signals. Peña and Kalnay (2004) have shown that in this case one can still take advantage of the longer time scale of the slow modes. Breeding with rescaling at longer intervals can identify the slower coupled mode (unlike linear singular vectors or Lyapunov vectors. which are linear, and select the fastest mode). Cai et al (2002) performed breeding with the Cane-Zebiak model

and used the bred vectors for simulated ensemble forecasting and data assimilation experiments, with verv encouraging results. Yang et al (2004) also obtained good results using the operational NAS NSIPP coupled GCM, and very similar results were obtained with an NCEP coupled GCM. These "perfect model" breeding experiments were done using a rescaling interval of one month and the Niño-3 SST anomalies as the rescaling norm. Results with the operational NSIPP coupled data assimilation system indicate that the growth rate and shape of coupled bred vectors in the Equatorial region is strongly related to the ENSO forecast error.

These results suggest that in coupled systems that contain fast and slow instabilities, it may not be possible to use the same EnKF approach to do data assimilation for both the fast and the slow processes. As in breeding, it may be necessary to choose different time intervals for the analysis of fast and slow instabilities.

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